

Accuplacer Study Modules

TOPIC: Factor Trinomials when the Leading Coefficient is NOT 1

Khan Academy Link:

<https://www.bing.com/videos/search?q=kahn+academy+factor+trinomial+lead+coefficient+is+not+1&view=detail&mid=08E4EE9C1D2F79DE09FB08E4EE9C1D2F79DE09FB&FORM=VIRE>

Follow the steps required for factoring trinomials when the leading coefficient is not 1:

- Step 1:** Make sure that the trinomial is written in the correct order; the trinomial must be written in **descending order** from highest power to lowest power.
- Step 2:** Decide if the three terms have anything in common, called the greatest common factor or GCF. If so, **factor out the GCF**. Do not forget to include the GCF as part of your final answer.
- Step 3:** **Multiply the leading coefficient and the constant**, that is multiply the first and last numbers together. In $ax^2 + bx + c$, these are the a and c values.
- Step 4:** **List all of the factors** of the product from Step 3. Give values the appropriate sign attending to rules of integers.
Reminder: $(+) \times (+) = (+)$ $(-) \times (-) = (+)$ $(-) \times (+) = (-)$ $(+) \times (-) = (-)$
- Step 5:** After choosing the **correct pair of numbers**, you must give each number a sign so that when they are combined they will **equal the number next to x (b value)** and also multiply to equal the product found in Step 3. The b value is the coefficient of x in $ax^2 + bx + c$.
- Step 6:** Rewrite the original problem with four terms by **splitting the middle term into the two numbers** chosen in step 5.
- Step 7:** Now that the problem is written with four terms, you can **factor by grouping**.

Sample problem: Factor $6x^2 - 4x - 16$ completely.

1. Make sure the trinomial is written in **descending order**. This trinomial is already written in descending order from highest to lowest power.
2. **Factor out the GCF** (Greatest Common Factor). The GCF of the three terms in this case is **2**.
 $2(3x^2 - 2x - 8)$
3. Multiply the lead coefficient (a value) and the constant (c value). $a = 3$ $c = -8$ **$3 \times -8 = -24$**
4. **List the factors** of the product from step 3.
 -1×24 -2×12 -3×8 -4×6
 1×-24 2×-12 3×-8 4×-6

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5. Choose the correct factor pair that multiplies to give you the product of the a and c values and have a sum that equal the b value. $a \times c = -24$ $b = -2$
- $-1 + 24 = 23$ $-2 + 12 = 10$ $-3 + 8 = 5$ $-4 + 6 = 2$
 $1 + -24 = -23$ $2 + -12 = -10$ $3 + -8 = -5$ $4 + -6 = -2$
6. Rewrite the original problem with four terms by splitting the middle term into the two numbers chosen in the previous step.
- $2(3x^2 \quad \quad -8)$ Substitute value from the previous step.
 $2(3x^2 + 4x - 6x - 8)$
7. Factor by grouping.
- $2(3x^2 + 4x)(-6x - 8)$
 $2(x(3x + 4) - 2(3x + 4))$
 $2(x-2)(3x+4)$

Now complete the four practice problems on the next page and check your answers!

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1. Factor $6x^2 + x - 2$ completely.

2. Factor $36x^3 + 33x^2 + 6x$ completely.

3. Factor $12x^2 - 29x + 15$ completely.

4. Factor $3x^2 - 3x - 90$ completely.